## SOLUTIONS TO CONCEPTS **CHAPTER 17**

1. Given that, 400 m <  $\lambda$  < 700 nm.

$$\frac{1}{700nm}<\frac{1}{\lambda}<\frac{1}{400nm}$$

$$\Rightarrow \frac{1}{7\times 10^{-7}} < \frac{1}{\lambda} < \frac{1}{4\times 10^{-7}} \Rightarrow \frac{3\times 10^8}{7\times 10^{-7}} < \frac{c}{\lambda} < \frac{3\times 10^8}{4\times 10^{-7}} \text{ (Where, c = speed of light = 3 \times 10^8 m/s)}$$

$$\Rightarrow 4.3 \times 10^{14} < c/\lambda < 7.5 \times 10^{14}$$

$$\Rightarrow$$
 4.3 × 10<sup>14</sup> Hz < f < 7.5 × 10<sup>14</sup> Hz.

2. Given that, for sodium light,  $\lambda = 589 \text{ nm} = 589 \times 10^{-9} \text{ m}$ 

a) 
$$f_a = \frac{3 \times 10^8}{589 \times 10^{-9}} = 5.09 \times 10^{14} \text{ sec}^{-1} \left[ \because f = \frac{c}{\lambda} \right]$$

b) 
$$\frac{\mu_a}{\mu_w} = \frac{\lambda_w}{\lambda_a} \Rightarrow \frac{1}{1.33} = \frac{\lambda_w}{589 \times 10^{-9}} \Rightarrow \lambda_w = 443 \text{ nm}$$

c)  $f_w = f_a = 5.09 \times 10^{14} \text{ sec}^{-1}$  [Frequency does not change]

d) 
$$\frac{\mu_a}{\mu_w} = \frac{v_w}{v_a} \Rightarrow v_w = \frac{\mu_a v_a}{\mu_w} = \frac{3 \times 10^8}{1.33} = 2.25 \times 10^8 \text{ m/sec.}$$

We know that,  $\frac{\mu_2}{\mu_1} = \frac{v_1}{v_2}$ 

So,  $\frac{1472}{1} = \frac{3 \times 10^8}{v_{400}} \Rightarrow v_{400} = 2.04 \times 10^8 \text{m/sec.}$ 

[because, for air,  $\mu = 1$  and  $v = 3 \times 10^8$  m/s

Again,  $\frac{1452}{1} = \frac{3 \times 10^8}{v_{760}} \Rightarrow v_{760} = 2.07 \times 10^8 \text{m/sec.}$ 

3. We know that,  $\frac{\mu_2}{\mu_1} = \frac{v_1}{v_2}$ 

So, 
$$\frac{1472}{1} = \frac{3 \times 10^8}{v_{400}} \Rightarrow v_{400} = 2.04 \times 10^8 \text{m/sec}$$

Again, 
$$\frac{1452}{1} = \frac{3 \times 10^8}{v_{760}} \Rightarrow v_{760} = 2.07 \times 10^8 \text{m/sec}$$

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4.  $\mu_t = \frac{1 \times 3 \times 10^8}{(2.4) \times 10^8} = 1.25 \left[ \text{since, } \mu = \frac{\text{velocity of light in vaccum}}{\text{velocity of light in the given medium}} \right]$ 

5. Given that,  $d = 1 \text{ cm} = 10^{-2} \text{ m}$ ,  $\lambda = 5 \times 10^{-7} \text{ m}$  and D = 1 m

a) Separation between two consecutive maxima is equal to fringe width.

So, 
$$\beta = \frac{\lambda D}{d} = \frac{5 \times 10^{-7} \times 1}{10^{-2}} \text{ m} = 5 \times 10^{-5} \text{ m} = 0.05 \text{ mm}.$$

b) When,  $\beta = 1 \text{ mm} = 10^{-3} \text{ m}$ 

$$10^{-3}$$
m =  $\frac{5 \times 10^{-7} \times 1}{D}$   $\Rightarrow$  D =  $5 \times 10^{-4}$  m = 0.50 mm.

Given that,  $\beta = 1 \text{ mm} = 10^{-3} \text{ m}$ , D = 2.t m and d = 1 mm =  $10^{-3} \text{ m}$ 

So, 
$$10^{-3}$$
m =  $\frac{25 \times \lambda}{10^{-3}} \Rightarrow \lambda = 4 \times 10^{-7}$  m = 400 nm.

7. Given that,  $d = 1 \text{ mm} = 10^{-3} \text{ m}$ , D = 1 m.

So, fringe with = 
$$\frac{D\lambda}{d}$$
 = 0.5 mm.

a) So, distance of centre of first minimum from centre of central maximum = 0.5/2 mm = 0.25 mm

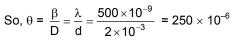
b) No. of fringes = 10 / 0.5 = 20.

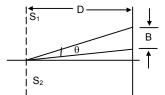
8. Given that,  $d = 0.8 \text{ mm} = 0.8 \times 10^{-3} \text{ m}$ ,  $\lambda = 589 \text{ nm} = 589 \times 10^{-9} \text{ m}$  and D = 2 m.

So, 
$$\beta = \frac{D\lambda}{d} = \frac{589 \times 10^{-9} \times 2}{0.8 \times 10^{-3}} = 1.47 \times 10^{-3} \text{ m} = 147 \text{ mm}.$$

Given that,  $\lambda = 500 \text{ nm} = 500 \times 10^{-9} \text{ m}$  and  $d = 2 \times 10^{-3} \text{ m}$ 

As shown in the figure, angular separation  $\theta = \frac{\beta}{D} = \frac{\lambda D}{dD} = \frac{\lambda}{d}$ 





- $= 25 \times 10^{-5}$  radian = 0.014 degree.
- 10. We know that, the first maximum (next to central maximum) occurs at  $y = \frac{\lambda D}{\Delta t}$

Given that,  $\lambda_1$  = 480 nm,  $\lambda_2$  = 600 nm, D = 150 cm = 1.5 m and d = 0.25 mm = 0.25 × 10<sup>-3</sup> m

So, 
$$y_1 = \frac{D\lambda_1}{d} = \frac{1.5 \times 480 \times 10^{-9}}{0.25 \times 10^{-3}} = 2.88 \text{ mm}$$
  
 $y_2 = \frac{1.5 \times 600 \times 10^{-9}}{0.25 \times 10^{-3}} = 3.6 \text{ mm}.$ 

So, the separation between these two bright fringes is given by,

- $\therefore$  separation =  $y_2 y_1 = 3.60 2.88 = 0.72 mm.$
- 11. Let m<sup>th</sup> bright fringe of violet light overlaps with n<sup>th</sup> bright fringe of red light.

$$\therefore \frac{m \times 400 nm \times D}{d} = \frac{n \times 700 nm \times D}{d} \Rightarrow \frac{m}{n} = \frac{7}{4}$$

- - Because, m/n = 7/4 = 14/8.

12. Let, t = thickness of the plate Given, optical path difference =  $(\mu - 1)t = \lambda/2$ 

$$\Rightarrow$$
 t =  $\frac{\lambda}{2(\mu - 1)}$ 

- 13. a) Change in the optical path =  $\mu t t = (\mu$ 
  - b) To have a dark fringe at the centre the pattern should shift by one half of a fringe.

$$\Rightarrow (\mu-1)t = \frac{\lambda}{2} \Rightarrow t = \frac{\lambda}{2(\mu-1)}.$$

14. Given that,  $\mu = 1.45$ , t = 0.02 mm =  $0.02 \times 10^{-3}$  m and  $\lambda = 620$  nm =  $620 \times 10^{-9}$  m

We know, when the transparent paper is pasted in one of the slits, the optical path changes by  $(\mu - 1)t$ . Again, for shift of one fringe, the optical path should be changed by  $\lambda$ .

So, no. of fringes crossing through the centre is given by,

$$n = \frac{(\mu - 1)t}{\lambda} = \frac{0.45 \times 0.02 \times 10^{-3}}{620 \times 10^{-9}} = 14.5$$

15. In the given Young's double slit experiment,

$$\mu$$
 = 1.6, t = 1.964 micron = 1.964 × 10<sup>-6</sup> m

We know, number of fringes shifted =  $\frac{(\mu - 1)t}{\lambda}$ 

So, the corresponding shift = No.of fringes shifted  $\times$  fringe width

$$= \frac{(\mu - 1)t}{\lambda} \times \frac{\lambda D}{d} = \frac{(\mu - 1)tD}{d} \qquad \dots (1)$$

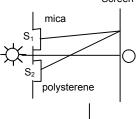
Again, when the distance between the screen and the slits is doubled.

Fringe width = 
$$\frac{\lambda(2D)}{d}$$
 ...(2)

From (1) and (2), 
$$\frac{(\mu - 1)tD}{d} = \frac{\lambda(2D)}{d}$$

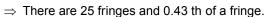
$$\Rightarrow \lambda = \frac{(\mu - 1)t}{\lambda} = \frac{(1.6 - 1) \times (1.964) \times 10^{-6}}{2} = 589.2 \times 10^{-9} = 589.2 \text{ nm}.$$

16. Given that,  $t_1$  =  $t_2$  = 0.5 mm = 0.5  $\times$  10<sup>-3</sup> m,  $\mu_m$  = 1.58 and  $\mu_p$  = 1.55,  $\lambda$  = 590 nm = 590  $\times$  10<sup>-9</sup> m, d = 0.12 cm = 12  $\times$  10<sup>-4</sup> m, D = 1 m



a) Fringe width = 
$$\frac{D\lambda}{d} = \frac{1 \times 590 \times 10^{-9}}{12 \times 10^{-4}} = 4.91 \times 10^{-4} \text{ m}.$$

- b) When both the strips are fitted, the optical path changes by  $\Delta x = (\mu_m - 1)t_1 - (\mu_p - 1)t_2 = (\mu_m - \mu_p)t$ =  $(1.58 - 1.55) \times (0.5)(10^{-3}) = 0.015 \times 10^{-13}$  m.
- So, No. of fringes shifted =  $\frac{0.015 \times 10^{-3}}{590 \times 10^{-3}}$  = 25.43.



⇒ There are 13 bright fringes and 12 dark fringes and 0.43 th of a dark fringe. So, position of first maximum on both sides will be given by

$$x = 0.43 \times 4.91 \times 10^{-4} = 0.021 \text{ cm}$$

$$x' = (1 - 0.43) \times 4.91 \times 10^{-4} = 0.028 \text{ cm (since, fringe width } = 4.91 \times 10^{-4} \text{ m)}$$

17. The change in path difference due to the two slabs is  $(\mu_1 - \mu_2)t$  (as in problem no. 16). For having a minimum at  $P_0$ , the path difference should change by  $\lambda/2$ .

So, 
$$\Rightarrow \lambda/2 = (\mu_1 - \mu_2)t \Rightarrow t = \frac{\lambda}{2(\mu_1 - \mu_2)}$$

- 18. Given that, t = 0.02 mm = 0.02  $\times$  10<sup>-3</sup> m,  $\mu_1$  = 1.45,  $\lambda$  = 600 nm = 600  $\times$  10<sup>-9</sup> m
  - a) Let,  $I_1$  = Intensity of source without paper = I
  - b) Then  $I_2$  = Intensity of source with paper = (4/9)I

$$\Rightarrow \frac{I_1}{I_2} = \frac{9}{4} \Rightarrow \frac{r_1}{r_2} = \frac{3}{2} \text{ [because I} \propto r^2\text{]}$$

where,  $r_1$  and  $r_2$  are corresponding amplitudes.

So, 
$$\frac{I_{max}}{I_{min}} = \frac{(r_1 + r_2)^2}{(r_1 - r_2)^2} = 25:1$$

b) No. of fringes that will cross the origin is given by,

$$n = \frac{(\mu - 1)t}{\lambda} = \frac{(1.45 - 1) \times 0.02 \times 10^{-3}}{600 \times 10^{-9}} = 15$$

 $n = \frac{(\mu - 1)t}{\lambda} = \frac{(1.45 - 1) \times 0.02 \times 10^{-3}}{600 \times 10^{-9}} = 15.$ 19. Given that, d = 0.28 mm = 0.28 × 10<sup>-3</sup> m, D = 48 cm = 0.48 m,  $\lambda_a$  = 700 nm in vacuum Let,  $\lambda_w$  = wavelength of red light in water

Since, the fringe width of the pattern is given by,

$$\beta = \frac{\lambda_w D}{d} = \frac{525 \times 10^{-9} \times 0.48}{0.28 \times 10^{-3}} = 9 \times 10^{-4} \text{ m} = 0.90 \text{ mm}.$$

20. It can be seen from the figure that the wavefronts reaching O from S<sub>1</sub> and S<sub>2</sub> will have a path difference of S<sub>2</sub>X.



$$\sin \theta = \frac{S_2 X}{S_1 S_2}$$



As the path difference is an odd multiple of  $\lambda/2$ , there will be a dark fringe at point P<sub>0</sub>.

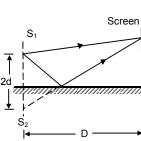
- 21. a) Since, there is a phase difference of  $\pi$  between direct light and reflecting light, the intensity just above the mirror will be zero.
  - b) Here, 2d = equivalent slit separation D = Distance between slit and screen.

We know for bright fringe, 
$$\Delta x = \frac{y \times 2d}{D} = n\lambda$$

But as there is a phase reversal of  $\lambda/2$ 

$$\Rightarrow \frac{y \times 2d}{D} + \frac{\lambda}{2} = n\lambda$$

$$\Rightarrow \frac{y \times 2d}{D} = n\lambda - \frac{\lambda}{2} \Rightarrow y = \frac{\lambda D}{4d}$$



 $S_2$ 

 $P_0$ 

22. Given that, D = 1 m,  $\lambda$  = 700 nm = 700  $\times$  10<sup>-9</sup> m

Since, a = 2 mm,  $d = 2a = 2 \text{mm} = 2 \times 10^{-3} \text{ m}$  (L loyd's mirror experiment)

Fringe width = 
$$\frac{\lambda D}{d} = \frac{700 \times 10^{-9} \, \text{m} \times 1\text{m}}{2 \times 10^{-3} \, \text{m}} = 0.35 \, \text{mm}.$$

23. Given that, the mirror reflects 64% of energy (intensity) of the light.

So, 
$$\frac{l_1}{l_2} = 0.64 = \frac{16}{25} \Rightarrow \frac{r_1}{r_2} = \frac{4}{5}$$

So, 
$$\frac{I_{\text{max}}}{I_{\text{min}}} = \frac{(r_1 + r_2)^2}{(r_1 - r_2)^2} = 81 : 1.$$

24. It can be seen from the figure that, the apparent distance of the screen from the slits is,

$$D = 2D_1 + D_2$$

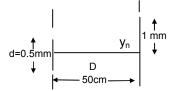
So, Fringe width = 
$$\frac{D\lambda}{d} = \frac{(2D_1 + D_2)\lambda}{d}$$

25. Given that,  $\lambda$  = (400 nm to 700 nm), d = 0.5 mm = 0.5  $\times$  10<sup>-3</sup> m,

D = 50 cm = 0.5 m and on the screen  $y_n = 1 \text{ mm} = 1 \times 10^{-3} \text{ m}$ 

a) We know that for zero intensity (dark fringe)

$$y_n = \left(\frac{2n+1}{2}\right) \frac{\lambda_n D}{d}$$
 where n = 0, 1, 2, ......



 $\Rightarrow \ \lambda_n = \frac{2}{(2n+1)} \frac{\lambda_n d}{D} = \frac{2}{2n+1} \times \frac{10^{-3} \times 0.5 \times 10^{-3}}{0.5} \Rightarrow \frac{2}{(2n+1)} \times 10^{-6} m = \frac{2}{(2n+1)} \times 10^3 nm$ 

If n = 1, 
$$\lambda_1$$
 = (2/3) × 1000 = 667 nm

If n = 1, 
$$\lambda_2$$
 = (2/5) × 1000 = 400 nm

So, the light waves of wavelengths 400 nm and 667 nm will be absent from the out coming light.

b) For strong intensity (bright fringes) at the hole

$$y_n = \frac{n\lambda_n D}{d} \Rightarrow \lambda_n = \frac{y_n d}{nD}$$

When, n = 1, 
$$\lambda_1 = \frac{y_n d}{D} = \frac{10^{-3} \times 0.5 \times 10^{-3}}{0.5} = 10^{-6} \text{m} = 1000 \text{nm}$$
.

1000 nm is not present in the range 400 nm - 700 nm

Again, where n = 2, 
$$\lambda_2 = \frac{y_n d}{2D}$$
 = 500 nm

So, the only wavelength which will have strong intensity is 500 nm.

26. From the diagram, it can be seen that at point O.

Path difference = (AB + BO) - (AC + CO)

= 2(AB - AC) [Since, AB = BO and AC = CO] = 
$$2(\sqrt{d^2 + D^2} - D)$$

For dark fringe, path difference should be odd multiple of  $\lambda/2$ .

So, 
$$2(\sqrt{d^2 + D^2} - D) = (2n + 1)(\lambda/2)$$

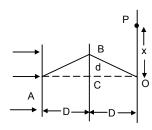
$$\Rightarrow \sqrt{d^2 + D^2} = D + (2n + 1) \lambda/4$$

$$\Rightarrow$$
 D<sup>2</sup> + d<sup>2</sup> = D<sup>2</sup> + (2n+1)<sup>2</sup>  $\lambda^2/16$  + (2n + 1)  $\lambda$ D/2

Neglecting,  $(2n+1)^2 \lambda^2/16$ , as it is very small

We get, d = 
$$\sqrt{(2n+1)\frac{\lambda D}{2}}$$

For minimum 'd', putting n = 0  $\Rightarrow$   $d_{min}$  =  $\sqrt{\frac{\lambda D}{2}}$  .



27. For minimum intensity

∴ 
$$S_1P - S_2P = x = (2n + 1) \lambda/2$$

From the figure, we get

$$\Rightarrow \ \sqrt{Z^2 + (2\lambda)^2} - Z = (2n+1)\frac{\lambda}{2}$$

$$\Rightarrow Z^2 + 4\lambda^2 = Z^2 + (2n+1)^2 \frac{\lambda^2}{4} + Z(2n+1)\lambda$$

$$\Rightarrow Z = \frac{4\lambda^2 - (2n+1)^2(\lambda^2/4)}{(2n+1)\lambda} = \frac{16\lambda^2 - (2n+1)^2\lambda^2}{4(2n+1)\lambda} \qquad \dots (1)$$

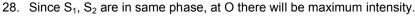
Putting, n = 
$$0 \Rightarrow Z = 15\lambda/4$$

$$n = -1 \Rightarrow Z = -15\lambda/4$$

$$n = 1 \Rightarrow Z = 7\lambda/12$$

$$n = 2 \Rightarrow Z = -9\lambda/20$$

 $\therefore$  Z =  $7\lambda/12$  is the smallest distance for which there will be minimum intensity.



Given that, there will be a maximum intensity at P.

$$\Rightarrow$$
 path difference =  $\Delta x = n\lambda$ 

From the figure,

$$(S_1P)^2 - (S_2P)^2 = (\sqrt{D^2 + X^2})^2 - (\sqrt{(D-2\lambda)^2 + X^2})^2$$

$$(S_1P)^2 - (S_2P)^2 = (\sqrt{D^2 + X^2})^2 - (\sqrt{(D - 2\lambda)^2 + X^2})^2$$

$$= 4\lambda D - 4\lambda^2 = 4 \lambda D (\lambda^2 \text{ is so small and can be neglected})$$

$$\Rightarrow S_1P - S_2P = \frac{4\lambda D}{2\sqrt{x^2 + D^2}} = n\lambda$$

$$\Rightarrow \frac{2D}{\sqrt{x^2 + D^2}} = v$$

$$\Rightarrow n^2 (X^2 + D^2) = 4D^2 = \Delta X = \frac{D}{n} \sqrt{4 - n^2}$$

$$\Rightarrow S_1P - S_2P = \frac{4\lambda D}{2\sqrt{x^2 + D^2}} = n\lambda$$

$$\Rightarrow \frac{2D}{\sqrt{x^2 + D^2}} = v$$

$$\Rightarrow n^2 (X^2 + D^2) = 4D^2 = \Delta X = \frac{D}{n} \sqrt{4 - n^2}$$

when n = 1, x = 
$$\sqrt{3}$$
 D

$$n = 2, x = 0$$

 $\therefore$  When X =  $\sqrt{3}$  D, at P there will be maximum intensity.

29. As shown in the figure,

$$(S_1P)^2 = (PX)^2 + (S_1X)^2$$
 ...(1)

$$(S_1P)^2 = (PX)^2 + (S_1X)^2$$
 ...(1  
 $(S_2P)^2 = (PX)^2 + (S_2X)^2$  ...(2

From (1) and (2),

$$(S_1P)^2 - (S_2P)^2 = (S_1X)^2 - (S_2X)^2$$
  
=  $(1.5 \lambda + R \cos \theta)^2 - (R \cos \theta - 15 \lambda)^2$ 

$$= 6λ R cos θ$$

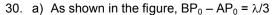
$$\Rightarrow (S_1P - S_2P) = \frac{6\lambda R\cos\theta}{2R} = 3\lambda\,\cos\,\theta.$$

For constructive interference,

$$(S_1P - S_2P)^2 = x = 3\lambda \cos \theta = n\lambda$$

$$\Rightarrow$$
 cos  $\theta$  = n/3  $\Rightarrow$   $\theta$  = cos<sup>-1</sup>(n/3), where n = 0, 1, 2, ....

 $\Rightarrow \theta = 0^{\circ}, 48.2^{\circ}, 70.5^{\circ}, 90^{\circ}$  and similar points in other quadrants.



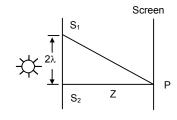
$$\Rightarrow \sqrt{(D^2 + d^2)} - D = \lambda/3$$

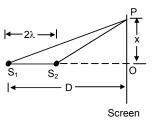
$$\Rightarrow$$
 D<sup>2</sup> + d<sup>2</sup> = D<sup>2</sup> + ( $\lambda^2$  / 9) + (2 $\lambda$ D)/3

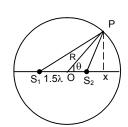
$$\Rightarrow$$
 d =  $\sqrt{(2\lambda D)/3}$  (neglecting the term  $\lambda^2/9$  as it is very small)

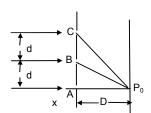
b) To find the intensity at P<sub>0</sub>, we have to consider the interference of light waves coming from all the three slits.

Here, 
$$CP_0 - AP_0 = \sqrt{D^2 + 4d^2} - D$$









$$= \sqrt{D^2 + \frac{8\lambda D}{3}} - D = D\left\{1 + \frac{8\lambda}{3D}\right\}^{1/2} - D$$

$$= D\left\{1 + \frac{8\lambda}{3D \times 2} + \dots\right\} - D = \frac{4\lambda}{3} \quad \text{[using binomial expansion]}$$

So, the corresponding phase difference between waves from C and A is,

$$\phi_{c} = \frac{2\pi x}{\lambda} = \frac{2\pi \times 4\lambda}{3\lambda} = \frac{8\pi}{3} = \left(2\pi + \frac{2\pi}{3}\right) = \frac{2\pi}{3}$$
 ...(1)

Again, 
$$\phi_B = \frac{2\pi x}{3\lambda} = \frac{2\pi}{3}$$
 ...(2)

So, it can be said that light from B and C are in same phase as they have some phase difference with respect to A.

So, R = 
$$\sqrt{(2r)^2 + r^2 + 2 \times 2r \times r \cos(2\pi/3)}$$
 (using vector method)  
=  $\sqrt{4r^2 + r^2 - 2r^2} = \sqrt{3r}$   
 $\therefore I_{P_0} - K(\sqrt{3r})^2 = 3Kr^2 = 3I$ 

As, the resulting amplitude is  $\sqrt{3}$  times, the intensity will be three times the intensity due to individual slits.

31. Given that,  $d = 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$ ,  $\lambda = 600 \text{ nm} = 6 \times 10^{-7} \text{ m}$ ,  $I_{\text{max}} = 0.20 \text{ W/m}^2$ , D = 2 mFor the point, y = 0.5 cm

We know, path difference = 
$$x = \frac{yd}{D} = \frac{0.5 \times 10^{-2} \times 2 \times 10^{-3}}{2} = 5 \times 10^{-6} \text{ m}$$

So, the corresponding phase difference is,

$$\phi = \frac{2\pi x}{\lambda} = \frac{2\pi \times 5 \times 10^{-6}}{6 \times 10^{-7}} \Rightarrow \frac{50\pi}{3} = 16\pi + \frac{2\pi}{3} \Rightarrow \phi = \frac{2\pi}{3}$$

A = 
$$\sqrt{r^2 + r^2 + 2r^2 \cos(2\pi/3)} = \sqrt{r^2 + r^2 - r^2} = r^2$$

So, the corresponding phase difference is, 
$$\phi = \frac{2\pi x}{\lambda} = \frac{2\pi \times 5 \times 10^{-6}}{6 \times 10^{-7}} \Rightarrow \frac{50\pi}{3} = 16\pi + \frac{2\pi}{3} \Rightarrow \phi = \frac{2\pi}{3}$$
 So, the amplitude of the resulting wave at the point  $y = 0.5$  cm is, 
$$A = \sqrt{r^2 + r^2 + 2r^2 \cos(2\pi/3)} = \sqrt{r^2 + r^2 - r^2} = r$$
 Since, 
$$\frac{1}{I_{max}} = \frac{A^2}{(2r)^2}$$
 [since, maximum amplitude = 2r] 
$$\Rightarrow \frac{1}{0.2} = \frac{A^2}{4r^2} = \frac{r^2}{4r^2}$$
 
$$\Rightarrow I = \frac{0.2}{4} = 0.05 \text{ W/m}^2.$$

32. i) When intensity is half the maximum  $\frac{1}{1} = \frac{1}{2}$ 

$$\Rightarrow \frac{4a^2\cos^2(\phi/2)}{4a^2} = \frac{1}{2}$$

$$\Rightarrow$$
  $\cos^2(\phi/2) = 1/2 \Rightarrow \cos(\phi/2) = 1/\sqrt{2}$ 

$$\Rightarrow \phi/2 = \pi/4 \Rightarrow \phi = \pi/2$$

$$\Rightarrow$$
 Path difference, x =  $\lambda/4$ 

$$\Rightarrow$$
 y = xD/d =  $\lambda$ D/4d

ii) When intensity is  $1/4^{th}$  of the maximum  $\frac{1}{1...} = \frac{1}{4}$ 

$$\Rightarrow \frac{4a^2\cos^2(\phi/2)}{4a^2} = \frac{1}{4}$$

$$\Rightarrow \cos^2(\phi/2) = 1/4 \Rightarrow \cos(\phi/2) = 1/2$$

$$\Rightarrow \phi/2 = \pi/3 \Rightarrow \phi = 2\pi/3$$

$$\Rightarrow$$
 Path difference, x =  $\lambda/3$ 

$$\Rightarrow$$
 y = xD/d =  $\lambda$ D/3d

33. Given that, D = 1 m, d = 1 mm =  $10^{-3}$  m,  $\lambda$  = 500 nm =  $5 \times 10^{-7}$  m For intensity to be half the maximum intensity.

$$y = \frac{\lambda D}{4d}$$
 (As in problem no. 32)

$$\Rightarrow y = \frac{5 \times 10^{-7} \times 1}{4 \times 10^{-3}} \Rightarrow y = 1.25 \times 10^{-4} \text{ m}.$$

34. The line width of a bright fringe is sometimes defined as the separation between the points on the two sides of the central line where the intensity falls to half the maximum.

We know that, for intensity to be half the maximum

$$y = \pm \frac{\lambda D}{4d}$$

$$\therefore \text{ Line width} = \frac{\lambda D}{4d} + \frac{\lambda D}{4d} = \frac{\lambda D}{2d}.$$

- 35. i) When,  $z = \lambda D/2d$ , at S<sub>4</sub>, minimum intensity occurs (dark fringe)
  - $\Rightarrow$  Amplitude = 0,
  - At  $S_3$ , path difference = 0
  - ⇒ Maximum intensity occurs.
  - $\Rightarrow$  Amplitude = 2r.
  - So, on  $\Sigma$ 2 screen,

$$\frac{I_{\text{max}}}{I_{\text{min}}} = \frac{(2r+0)^2}{(2r-0)^2} = 1$$

- ii) When,  $z = \lambda D/2d$ , At S<sub>4</sub>, minimum intensity occurs. (dark fringe)
- $\Rightarrow$  Amplitude = 0.
- At  $S_3$ , path difference = 0
- ⇒ Maximum intensity occurs.
- $\Rightarrow$  Amplitude = 2r.
- So, on  $\Sigma$ 2 screen,

$$\frac{I_{\text{max}}}{I_{\text{min}}} = \frac{(2r + 2r)^2}{(2r - 0)^2} = \infty$$

- iii) When,  $z = \lambda D/4d$ , At S<sub>4</sub>, intensity = I<sub>max</sub> / 2
- $\Rightarrow$  Amplitude =  $\sqrt{2r}$ .
- ∴ At S<sub>3</sub>, intensity is maximum.
- $\Rightarrow$  Amplitude = 2r

$$\therefore \ \frac{I_{max}}{I_{min}} = \frac{(2r + \sqrt{2r})^2}{(2r - \sqrt{2r})^2} = 34.$$

36. a) When,  $z = D\lambda/d$ 

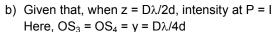
So, 
$$OS_3 = OS_4 = D\lambda/2d \Rightarrow Dark$$
 fringe at  $S_3$  and  $S_4$ .

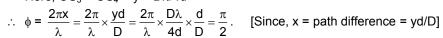
 $\Rightarrow$  At S<sub>3</sub>, intensity at S<sub>3</sub> = 0  $\Rightarrow$  I<sub>1</sub> = 0

At S<sub>4</sub>, intensity at S<sub>4</sub> = 
$$0 \Rightarrow I_2 = 0$$

At P, path difference =  $0 \Rightarrow$  Phase difference = 0.

$$\Rightarrow$$
 I = I<sub>1</sub> + I<sub>2</sub> +  $\sqrt{I_1I_2}$  cos 0° = 0 + 0 + 0 = 0  $\Rightarrow$  Intensity at P = 0.

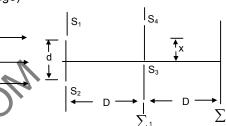






So, 
$$I' + I' + 2I' \cos 0^\circ = I$$
.

$$\Rightarrow$$
 4I' = I  $\Rightarrow$  I' = 1/4.



When, 
$$z = \frac{3D\lambda}{2d}$$
,  $\Rightarrow y = \frac{3D\lambda}{4d}$ 

$$\therefore \ \varphi = \frac{2\pi x}{\lambda} = \frac{2\pi}{\lambda} \times \frac{yd}{D} = \frac{2\pi}{\lambda} \times \frac{3D\lambda}{4d} \times \frac{d}{D} = \frac{3\pi}{2}$$

Let, I" be the intensity at S<sub>3</sub> and S<sub>4</sub> when,  $\phi = 3\pi/2$ Now comparing,

$$\frac{I''}{I} = \frac{a^2 + a^2 + 2a^2 \cos(3\pi/2)}{a^2 + a^2 + 2a^2 \cos(\pi/2)} = \frac{2a^2}{2a^2} = 1 \qquad \Rightarrow I'' = I' = I/4.$$

:. Intensity at P =  $1/4 + 1/4 + 2 \times (1/4) \cos 0^{\circ} = 1/2 + 1/2 = 1$ .

c) When 
$$z = 2D\lambda/d$$

$$\Rightarrow$$
 y = OS<sub>3</sub> = OS<sub>4</sub> = D $\lambda$ /d

$$\therefore \quad \phi = \frac{2\pi x}{\lambda} = \frac{2\pi}{\lambda} \times \frac{yd}{D} = \frac{2\pi}{\lambda} \times \frac{D\lambda}{d} \times \frac{d}{D} = 2\pi .$$

$$\frac{I'''}{I'} = \frac{a^2 + a^2 + 2a^2 \cos 2\pi}{a^2 + a^2 + 2a^2 \cos \pi/2} = \frac{4a^2}{2a^2} = 2$$

$$\Rightarrow$$
 I''' = 2I' = 2(I/4) = I/2

At P,  $I_{resultant} = I/2 + I/2 + 2(I/2) \cos 0^{\circ} = I + I = 2I$ .

So, the resultant intensity at P will be 2I.

## 37. Given $d = 0.0011 \times 10^{-3} \text{ m}$

For minimum reflection of light,  $2\mu d = n\lambda$ 

$$\Rightarrow \ \mu = \frac{n\lambda}{2d} = \frac{2n\lambda}{4d} = \frac{580 \times 10^{-9} \times 2n}{4 \times 11 \times 10^{-7}} = \frac{5.8}{44} (2n) = 0.132 \ (2n)$$

Given that,  $\mu$  has a value in between 1.2 and 1.5. ⇒ When, n = 5,  $\mu = 0.132 \times 10 = 1.32$ .

38. Given that,  $\lambda = 560 \times 10^{-9}$  m,  $\mu = 1.4$ .

$$\Rightarrow$$
 When, n = 5,  $\mu$  = 0.132 × 10 = 1.32

38. Given that 
$$\lambda = 560 \times 10^{-9}$$
 m  $\mu = 1.4$ 

For strong reflection, 
$$2\mu d = (2n + 1)\lambda/2 \Rightarrow d = \frac{(2n + 1)\lambda}{4d}$$
  
For minimum thickness, putting  $n = 0$ .

$$\Rightarrow$$
 d =  $\frac{\lambda}{4d}$   $\Rightarrow$  d =  $\frac{560 \times 10^{-9}}{14}$   $\Rightarrow$  10<sup>-7</sup> m = 100 nm.

39. For strong transmission, 2 
$$\mu d = n\lambda \implies \lambda = \frac{2\mu d}{n}$$

Given that, 
$$\mu = 1.33$$
,  $d = 1 \times 10^{-4}$  cm =  $1 \times 10^{-6}$  m.  

$$\Rightarrow \lambda = \frac{2 \times 1.33 \times 1 \times 10^{-6}}{n} = \frac{2660 \times 10^{-9}}{n} m$$

when,

$$n = 4$$
,  $\lambda_1 = 665$  nm

$$n = 5$$
,  $\lambda_2 = 532 \text{ nm}$ 

$$n = 6$$
,  $\lambda_3 = 443$  nm

40. For the thin oil film,

$$d = 1 \times 10^{-4}$$
 cm =  $10^{-6}$  m,  $\mu_{oil} = 1.25$  and  $\mu_x = 1.50$ 

$$\lambda = \frac{2\mu d}{(n+1/2)} \frac{2 \times 10^{-6} \times 1.25 \times 2}{2n+1} = \frac{5 \times 10^{-6} m}{2n+1}$$

$$\Rightarrow \lambda = \frac{5000 \text{ nm}}{2n+1}$$

For the wavelengths in the region (400 nm - 750 nm)

When, n = 3, 
$$\lambda = \frac{5000}{2 \times 3 + 1} = \frac{5000}{7} = 714.3 \text{ nm}$$

When, n = 4, 
$$\lambda = \frac{5000}{2 \times 4 + 1} = \frac{5000}{9} = 555.6 \text{ nm}$$
  
When, n = 5,  $\lambda = \frac{5000}{2 \times 5 + 1} = \frac{5000}{11} = 454.5 \text{ nm}$ 

41. For first minimum diffraction, b sin  $\theta = \lambda$ 

Here, 
$$\theta = 30^{\circ}$$
, b = 5 cm

∴ 
$$\lambda = 5 \times \sin 30^{\circ} = 5/2 = 2.5$$
 cm.

42. 
$$\lambda = 560 \text{ nm} = 560 \times 10^{-9} \text{ m}, b = 0.20 \text{ mm} = 2 \times 10^{-4} \text{ m}, D = 2 \text{ m}$$

Since, R = 
$$1.22 \frac{\lambda D}{b} = 1.22 \times \frac{560 \times 10^{-9} \times 2}{2 \times 10^{-4}} = 6.832 \times 10^{-3} \text{ M} = 0.683 \text{ cm}.$$

So, Diameter = 2R = 1.37 cm.

43.  $\lambda = 620 \text{ nm} = 620 \times 10^{-9} \text{ m},$ 

D = 20 cm = 
$$20 \times 10^{-2}$$
 m, b = 8 cm =  $8 \times 10^{-2}$  m

$$\therefore R = 1.22 \times \frac{620 \times 10^{-4} \times 20 \times 10^{-2}}{8 \times 10^{-2}} = 1891 \times 10^{-9} = 1.9 \times 10^{-6} \text{ m}$$

So, diameter = 
$$2R = 3.8 \times 10^{-6} \text{ m}$$

